Gravity in three dimensions The AdS₃/LCFT₂ correspondence

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Outline

Introduction to 3D gravity

Topologically massive gravity

Logarithmic CFT conjecture

Consequences, Generalizations & Applications

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- ► Quantum gravity
 - Address conceptual issues of quantum gravity
 - ▶ Black hole evaporation, information loss, black hole microstate counting, virtual black hole production, ...
 - ► Technically much simpler than 4D or higher D gravity
 - ► Integrable models: powerful tools in physics (Coulomb problem, Hydrogen atom, harmonic oscialltor, ...)
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- ► Gauge/gravity duality
 - Deeper understanding of black hole holography
 - AdS₃/CFT₂ correspondence best understood
 - Quantum gravity via AdS/CFT? (Witten '07, Li, Song, Strominger '08)
 - Applications to 2D condensed matter systems?
 - Gauge gravity duality beyond standard AdS/CFT: warped AdS, asymptotic Lifshitz, non-relativistic CFTs, logarithmic CFTs, ...

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- Physics
 - Cosmic strings (Deser, Jackiw, 't Hooft '84, '92)
 - ▶ Black hole analog systems in condensed matter physics (graphene, BEC, fluids, ...)

- ▶ 11D: 1210 (1144 Weyl and 66 Ricci)
- ▶ 10D: 825 (770 Weyl and 55 Ricci)
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- ▶ 3D: lowest dimension exhibiting BHs and gravitons
- ▶ Simplest gravitational theories with BHs and gravitons in 3D

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Action and equations of motion of topologically massive gravity (TMG)

Consider the action (Deser, Jackiw & Templeton '82)

$$I_{\rm TMG} = \frac{1}{16\pi G} \int \mathrm{d}^3 x \sqrt{-g} \left[R + \frac{2}{\ell^2} + \frac{1}{2\mu} \varepsilon^{\lambda\mu\nu} \Gamma^{\rho}{}_{\lambda\sigma} \left(\partial_{\mu} \Gamma^{\sigma}{}_{\nu\rho} + \frac{2}{3} \Gamma^{\sigma}{}_{\mu\tau} \Gamma^{\tau}{}_{\nu\rho} \right) \right]$$

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Equations of motion:

$$R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R - \frac{1}{\ell^2} g_{\mu\nu} + \frac{1}{\mu} C_{\mu\nu} = 0$$

with the Cotton tensor defined as

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Some properties of TMG

- Massive gravitons and black holes
- ▶ AdS solutions and asymptotic AdS solutions
- warped AdS solutions and warped AdS black holes
- ► Lifshitz solutions and Lifshitz pp-waves

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Reduced action (Clement '94):

$$I_{\rm C}[e,X^i] \sim \int \mathrm{d}\rho \, e \left[\frac{1}{2} \, e^{-2} \dot{X}^i \dot{X}^j \eta_{ij} - \frac{2}{\ell^2} + \frac{1}{2\mu} \, e^{-3} \, \epsilon_{ijk} \, X^i \dot{X}^j \ddot{X}^k \right]$$

Here e is the Einbein and $X^i=(T,X,Y)$ a Lorentzian 3-vector

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Here e is the Einbein and $X^i=(T,X,Y)$ a Lorentzian 3-vector Classification of solutions:

- Einstein solutions: AdS, BTZ
- warped solutions: warped AdS, warped black holes
- Lifshitz solutions: zero modes of asymptotic Lifshitz pp-waves
- ▶ other solutions? (Ertl, Grumiller, Johansson, in prep.)

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$$\mu \ell = 1$$

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Calculating the central charges of the dual boundary CFT yields

$$c_L = \frac{3\ell}{2G} \left(1 - \frac{1}{\mu \ell} \right) \qquad c_R = \frac{3\ell}{2G} \left(1 + \frac{1}{\mu \ell} \right)$$

Thus, at the chiral point we get

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- ► Abbreviate "Cosmological TMG at the chiral point" as CCTMG
- CCTMG is also known as "chiral gravity"
- ▶ Dual CFT: chiral? (conjecture by Li, Song & Strominger '08)
- More adequate name for CCTMG: "logarithmic gravity"

Linearization around AdS background.

$$g_{\mu\nu} = \bar{g}_{\mu\nu} + h_{\mu\nu}$$

Line-element $\bar{g}_{\mu\nu}$ of pure AdS:

$$d\bar{s}_{AdS}^{2} = \bar{g}_{\mu\nu} dx^{\mu} dx^{\nu} = \ell^{2} (-\cosh^{2}\rho d\tau^{2} + \sinh^{2}\rho d\phi^{2} + d\rho^{2})$$

Isometry group: $SL(2,\mathbb{R})_L \times SL(2,\mathbb{R})_R$

Useful to introduce light-cone coordinates $u = \tau + \phi$, $v = \tau - \phi$.

The $SL(2,\mathbb{R})_L$ generators

$$L_0 = i\partial_u$$

$$L_{\pm 1} = ie^{\pm iu} \left[\frac{\cosh 2\rho}{\sinh 2\rho} \partial_u - \frac{1}{\sinh 2\rho} \partial_v \mp \frac{i}{2} \partial_\rho \right]$$

obey the algebra $[L_0,L_{\pm 1}]=\mp L_{\pm 1}$, $[L_1,L_{-1}]=2L_0$.

The $SL(2,\mathbb{R})_R$ generators $\bar{L}_0,\bar{L}_{\pm 1}$ obey same algebra, but with

$$u \leftrightarrow v$$
, $L \leftrightarrow \bar{L}$

Linearization around AdS background.

$$g_{\mu\nu} = \bar{g}_{\mu\nu} + h_{\mu\nu}$$

leads to linearized EOM that are third order PDE

$$G_{\mu\nu}^{(1)} + \frac{1}{\mu} C_{\mu\nu}^{(1)} = (\mathcal{D}^R \mathcal{D}^L \mathcal{D}^M h)_{\mu\nu} = 0$$
 (1)

with three mutually commuting first order operators

$$(\mathcal{D}^{L/R})_{\mu}{}^{\nu} = \delta_{\mu}^{\nu} \pm \ell \, \varepsilon_{\mu}{}^{\alpha\nu} \bar{\nabla}_{\alpha} \qquad (\mathcal{D}^{M})_{\mu}{}^{\nu} = \delta_{\mu}^{\nu} + \frac{1}{\mu} \varepsilon_{\mu}{}^{\alpha\nu} \bar{\nabla}_{\alpha}$$

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Three linearly independent solutions to (1):

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At chiral point left (L) and massive (M) branches coincide!

Li, Song & Strominger found all normalizable solutions of linearized EOM.

lacktriangle Primaries: $L_0, ar{L}_0$ eigenstates $\psi^{L/R/M}$ with

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▶ At chiral point: *L* and *M* branches degenerate. Get log solution (Grumiller & Johansson '08)

$$\psi_{\mu\nu}^{\log} = \lim_{\mu\ell \to 1} \frac{\psi_{\mu\nu}^{M}(\mu\ell) - \psi_{\mu\nu}^{L}}{\mu\ell - 1}$$

with property

$$(\mathcal{D}^L \psi^{\log})_{\mu\nu} = (\mathcal{D}^M \psi^{\log})_{\mu\nu} \neq 0, \qquad ((\mathcal{D}^L)^2 \psi^{\log})_{\mu\nu} = 0$$

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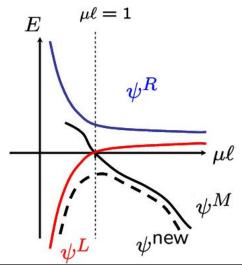
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- With signs as defined in Carlip, Deser, Waldron, Wise '08: BHs negative energy, gravitons positive energy
- Either way need a mechanism to eliminate unwanted negative energy objects — either the gravitons or the BHs
- Even at chiral point the problem persists because of the logarithmic mode. See Figure. (thanks to Niklas Johansson)

Energy for all branches:



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Motivating the conjecture

Log mode exhibits interesting property:

$$H\begin{pmatrix} \psi^{\log} \\ \psi^L \end{pmatrix} = \begin{pmatrix} 2 & 1 \\ 0 & 2 \end{pmatrix} \begin{pmatrix} \psi^{\log} \\ \psi^L \end{pmatrix}$$
$$J\begin{pmatrix} \psi^{\log} \\ \psi^L \end{pmatrix} = \begin{pmatrix} 2 & 0 \\ 0 & 2 \end{pmatrix} \begin{pmatrix} \psi^{\log} \\ \psi^L \end{pmatrix}$$

Here $H=L_0+\bar{L}_0\sim\partial_t$ is the Hamilton operator and $J=L_0-\bar{L}_0\sim\partial_\phi$ the angular momentum operator.

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CCTMG dual to a logarithmic CFT (Grumiller, Johansson '08)

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► Logarithmic mode is asymptotically AdS

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- ▶ Brown-York stress tensor is finite and traceless, but not chiral
- ► Log mode persists non-perturbatively, as shown by Hamilton analysis (Grumiller, Jackiw & Johansson '08, Carlip '08)

▶ Any CFT has a conserved traceless energy momentum tensor.

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▶ The 2- and 3-point correlators are fixed by conformal Ward identities.

$$\begin{split} \langle \mathcal{O}^R(\bar{z}) \, \mathcal{O}^R(0) \rangle &= \frac{c_R}{2\bar{z}^4} \\ \langle \mathcal{O}^L(z) \, \mathcal{O}^L(0) \rangle &= \frac{c_L}{2z^4} \\ \langle \mathcal{O}^L(z) \, \mathcal{O}^R(0) \rangle &= 0 \\ \langle \mathcal{O}^R(\bar{z}) \, \mathcal{O}^R(\bar{z}') \, \mathcal{O}^R(0) \rangle &= \frac{c_R}{\bar{z}^2 \bar{z}'^2 (\bar{z} - \bar{z}')^2} \\ \langle \mathcal{O}^L(z) \, \mathcal{O}^L(z') \, \mathcal{O}^L(0) \rangle &= \frac{c_L}{z^2 z'^2 (z - z')^2} \\ \langle \mathcal{O}^L(z) \, \mathcal{O}^R(\bar{z}') \, \mathcal{O}^R(0) \rangle &= 0 \\ \langle \mathcal{O}^L(z) \, \mathcal{O}^L(z') \, \mathcal{O}^R(0) \rangle &= 0 \end{split}$$

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- ▶ The 2- and 3-point correlators are fixed by conformal Ward identities. Central charges $c_{L/R}$ determine key properties of CFT.
- ▶ Suppose there is an additional operator \mathcal{O}^M with conformal weights $h=2+\varepsilon, \ \bar{h}=\varepsilon$

$$\langle \mathcal{O}^M(z,\bar{z}) \, \mathcal{O}^M(0,0) \rangle = \frac{\hat{B}}{z^{4+2\varepsilon} \bar{z}^{2\varepsilon}}$$

which degenerates with \mathcal{O}^{L} in limit $c_L \propto arepsilon o 0$

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$$\langle \mathcal{O}^M(z,\bar{z}) \, \mathcal{O}^M(0,0) \rangle = \frac{\hat{B}}{z^{4+2\varepsilon} \bar{z}^{2\varepsilon}}$$

which degenerates with \mathcal{O}^{L} in limit $c_L \propto arepsilon o 0$

► Then energy momentum tensor acquires logarithmic partner \mathcal{O}^{\log}

$$\mathcal{O}^{\log} = b_L \frac{\mathcal{O}^L}{c_L} + \frac{b_L}{2} \mathcal{O}^M$$

where

$$\mathbf{b_L} := \lim_{c_L \to 0} -\frac{c_L}{\varepsilon} \neq 0$$

▶ Any CFT has a conserved traceless energy momentum tensor.

$$T_{z\bar{z}} = 0$$
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- ► Some 2-point correlators:

$$\begin{split} &\langle \mathcal{O}^L(z)\mathcal{O}^L(0,0)\rangle = 0\\ &\langle \mathcal{O}^L(z)\mathcal{O}^{\log}(0,0)\rangle = \frac{b_L}{2z^4}\\ &\langle \mathcal{O}^{\log}(z,\bar{z})\mathcal{O}^{\log}(0,0)\rangle = -\frac{b_L\ln\left(m_L^2|z|^2\right)}{z^4} \end{split}$$

"New anomaly" b_L determines key properties of logarithmic CFT.

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 Calculate non-normalizable modes for left, right and logarithmic branches by solving linearized EOM on gravity side

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- ► Works at level of 2-point correlators (Skenderis, Taylor & van Rees '09, Grumiller & Sachs '09)
- ▶ Works at level of 3-point correlators (Grumiller & Sachs '09)
- ▶ Value of new anomaly: $b_L = -c_R = -3\ell/G$

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Conclusion: all consistency tests show validity of LCFT conjecture!

Outline

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Topologically massive gravity

Logarithmic CFT conjecture

Consequences, Generalizations & Applications

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If conjecture true: first example of $AdS_3/LCFT_2$ correspondence!

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Not clear yet if chiral gravity exists!

If it exists: excellent toy model for quantum gravity!

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New massive gravity (Bergshoeff, Hohm & Townsend '09):

$$I_{\rm NMG} = \frac{1}{16\pi G} \int {\rm d}^3 x \sqrt{-g} \left[\sigma R + \frac{1}{m^2} \left(R^{\mu\nu} R_{\mu\nu} - \frac{3}{8} \, R^2 \right) - 2 \lambda m^2 \right]$$

Similar story (Grumiller & Hohm '09, Alishahiha & Naseh '10):

▶ Linearized EOM around AdS₃ $(g = \bar{g} + h)$

$$\left(\mathcal{D}^R\mathcal{D}^L\mathcal{D}^M\mathcal{D}^{\bar{M}}h\right)_{\mu\nu}=0$$

- ▶ Logarithmic point for $\lambda = 3$: $c_L = c_R = 0$
- Massive modes degenerate with left and right boundary gravitons
- ▶ 2-point correlators on gravity side match precisely those of a LCFT
- New anomalies: $b_L = b_R = -\sigma 12\ell/G$

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- ► Apply AdS₃/LCFT₂ to describe strongly coupled LCFTs!

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Thanks for your attention!



Some literature

- M. R. Gaberdiel, "An algebraic approach to logarithmic conformal field theory," Int. J. Mod. Phys. A18 (2003) 4593 hep-th/0111260.
- D. Grumiller and N. Johansson, "Gravity duals for logarithmic conformal field theories," 1001.0002. See also Refs. therein.
- W. Li, W. Song and A. Strominger, "Chiral Gravity in Three Dimensions," JHEP **0804** (2008) 082, 0801.4566.
- D. Grumiller and N. Johansson, "Instability in cosmological topologically massive gravity at the chiral point," JHEP **0807** (2008) 134, 0805.2610.
- K. Skenderis, M. Taylor and B. C. van Rees, "Topologically Massive Gravity and the AdS/CFT Correspondence," JHEP **0909** (2009) 045 0906.4926.
- D. Grumiller and I. Sachs, "AdS₃/LCFT₂ Correlators in Cosmological Topologically Massive Gravity," JHEP **1003** (2010) 012 0910.5241.