# Model for gravity at large distances

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# Outline

# Life, the Universe and Everything (we know) Particle Physics Cosmology

#### Puzzles

Energy budget of the Universe Dark matter

Model for Gravity at Large Distances As simple as possible, but not simpler Rindler force Observations

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- That's it! (well, almost...)

Standard Model of Particle Physics

A theory of (almost) everything:



Standard Model (SM) Lagrange density  $F_{\mu\nu}$ : bosons,  $\Psi$ : fermions,  $\Phi$ : Higgs

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  e.g. gyromagnetic ratio of μ Experiment (2002):

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Theory (2009):

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Currently SM improved at LHC



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► Tested to high accuracy: Perihelion shifts  $(\beta - 1 < 2 \cdot 10^{-4})$ Radar echo delay  $(\gamma - 1 < 2 \cdot 10^{-5})$ Binary pulsars  $(\alpha_3 < 4 \cdot 10^{-20})$ 

Life, the Universe and Everything (we know)

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Particle in the SM not found yet:



Higgs particle! (or whatever causes electro-weak symmetry breaking...) LHC will find it this decade!

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Further particles beyond SM? Inflaton?, SUSY?, Axions?, Dark Spinors?, Kaluza–Kleins?, ... LHC and Astro/Astroparticle--physics may find clues!





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- COBE (1989-1993), WMAP (since 2001), Planck (since 2009)





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#### CMB:



Above: COBE satellite (900km) Below: WMAP satellite at Lagrange point L2  $(1.5 * 10^6$ km)

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- E.g. energy densities know within %-range: Ω<sub>b</sub>, Ω<sub>ν</sub>, Ω<sub>γ</sub>, Ω<sub>m</sub>, Ω<sub>Λ</sub>, ... (baryons, neutrinos, radiation, matter, cosmological constant, ...)

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- Currently many experiments!



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Is anything else missing?



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- Less plausible, but logically possible: dark matter is gravitational effect



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To address these issues we need to understand GRAVITY AT LARGE DISTANCES!

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Neptune:



 1821: Alexis Bouvard published tables of orbit of Uranus

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Discovery of Neptune was first success of the Dark Matter concept!

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(picture based on

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Non-discovery of Vulcan was first failure of the Dark Matter concept!

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► Galactic rotation curves (pictures by Wikipedia)



#### A = Theory, B = Observation

### Astrophysics Modern gravitational anomalies

Anomalies = differences between theory and observations Prominent examples:

- Galactic rotation curves
- Pioneer anomaly? (pictures by NASA)



#### Anomalous acceleration towards the Sun?

Some crucial facts about the Dark Side of life:

 Fact 1: Vulcan scenario seems unlikely for Dark Matter, but cannot be excluded



MOND, TeVeS, modified theories of gravity, ...

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- Fact 2: Neptune scenario seems likely, but Dark Matter has not been detected (yet)



LSP, axion, WIMP, MACHO, ELKO, ...

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Possible strategies to make progress:

- Show that Vulcan scenario is correct
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Both strategies are currently out of reach!

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My strategy: remain agnostic and rephrase the question

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Key question:

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$$F/m = -M/r^2 + \ell^2/r^3 - 3M\ell^2/r^4 + \Lambda r - \frac{a}{a} \left(1 - \ell^2/r^2\right)$$

New force arises in this model!

Write down most general line-element compatible with spherical symmetry

$$\mathrm{d}s^2 = g_{\alpha\beta} \, \mathrm{d}x^\alpha \, \mathrm{d}x^\beta + \Phi^2 \, \mathrm{d}\Omega_{S^2}^2$$

Described by 2d metric g and scalar field  $\Phi$ . Use 2d theory to describe these fields!

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$$S = \int \mathrm{d}^2 x \sqrt{-g} \left[ f(\Phi) R + 2(\partial \Phi)^2 - 2V(\Phi) \right]$$

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Require absence of curvature singularities for large  $\Phi$ .

$$V = \Lambda \Phi^2 + \mathbf{a} \Phi + 1 + \mathcal{O}(1/\Phi)$$

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Solve equations of motion and get as most general solution  $\Phi = r$ ,

$$g_{\alpha\beta} \, \mathrm{d}x^{\alpha} \, \mathrm{d}x^{\beta} = -K^2 \, \mathrm{d}t^2 + \frac{\mathrm{d}r^2}{K^2} \qquad K^2 = 1 - \frac{2M}{r} - \Lambda r^2 + 2ar$$

New force at large distances Test this for galaxies

Choose some value for Rindler force *a*:

$$F/m = -M/r^2 - a$$





#### Note: *a* is positive!

New force at large distances Test this for Pioneer anomaly

Choose some value for Rindler force *a*:

$$F/m = -M/r^2 - a$$

Matches the Pioneer trajectory!



#### Note: *a* is positive!

D. Grumiller - Model for gravity at large distances

Model for Gravity at Large Distances

Scrutinize solar system data to get bounds on Rindler acceleration

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Bounds from perihelion shifts:

$$|a| < 2 \cdot 10^{-14} m/s^2$$

Last bound comes with caveats, however!

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- Alternatively, perhaps we do not fully understand gravity at very large distances

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- What determines magnitude of Rindler acceleration?
- Microscopic model predicting Rindler term? Where does it come from?

#### Thank you for your attention!



D. Grumiller — Model for gravity at large distances





#### Model for Gravity at Large Distances

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# ... questions?