# Flat space higher spin holography

Daniel Grumiller

Institute for Theoretical Physics TU Wien

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based on work w. Afshar, Bagchi, Basu, Detournay, Fareghbal, Gary, Riegler, Rosseel, Salzer, Sarkar, Schöller, Simon, ...

# Outline

Motivations

Holography basics

Flat space holography

Flat space higher spin holography

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Quantum gravity

Address conceptual issues of quantum gravity





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- Black holes (thermodynamics, evaporation, information loss, microstate counting, entanglement entropy, firewalls, ...)



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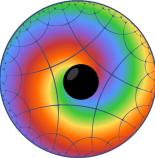
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- Holography
  - Holographic principle realized in Nature? (yes/no)



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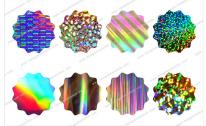
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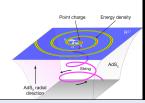
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- Applications
  - Gauge gravity correspondence (plasmas, condensed matter, ...)



Daniel Grumiller — Flat space higher spin holography

Motivations

## Specific motivation for 3D

Gravity in 3D is simpler than in higher dimensions

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Specific motivation for flat space higher spin gravity

Massless higher spin theories constrained by no-gos!

- Coleman–Mandula '67
- Aragone–Deser '79
- Weinberg–Witten '80
- recent summary: Bekaert, Boulanger, Sundell '12

Conclusion: there are no consistent interacting massless higher spin theories in 4- (or higher-) dimensional flat space

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Circumventing no-gos:

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Circumventing no-gos:

- Vasiliev '87-'90: higher spin theories in (A)dS
- Afshar, Bagchi, Fareghbal, DG, Rosseel '13; Gonzalez, Matulich, Pino, Troncoso '13: flat space higher spin theories in 3d

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Address these issues in 3D!



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Interesting generic constraints from CFT<sub>2</sub>! e.g. Hellerman '09, Hartman, Keller, Stoica '14

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Caveat: while there are many string compactifications with  $AdS_3$  factor, applying holography just to  $AdS_3$  factor does not capture everything!

Universal recipe:

1. Identify bulk theory and variational principle

Example: Einstein gravity with Dirichlet boundary conditions

$$I = -\frac{1}{16\pi G_N} \int \mathrm{d}^3 x \sqrt{|g|} \left(R + \frac{2}{\ell^2}\right)$$

with  $\delta g = {\rm fixed}$  at the boundary

Universal recipe:

wit

- $1. \ \mbox{Identify bulk theory and variational principle}$
- 2. Fix background and impose suitable boundary conditions Example: asymptotically AdS

$$\mathrm{d}s^2 = \mathrm{d}\rho^2 + \left(e^{2\rho/\ell}\gamma_{ij}^{(0)} + \gamma_{ij}^{(2)} + \dots\right)\,\mathrm{d}x^i\,\mathrm{d}x^j$$
  
h  $\delta\gamma^{(0)} = 0$  for  $\rho \to \infty$ 

Universal recipe:

- 1. Identify bulk theory and variational principle
- 2. Fix background and impose suitable boundary conditions
- 3. Perform canonical analysis and check consistency of bc's
  - Find and classify all constraints
  - Construct canonical gauge generators
  - Add boundary terms and get (variation of) canonical charges
  - Check integrability of canonical charges
  - Check finiteness of canonical charges
  - Check conservation (in time) of canonical charges
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Example: Brown-Henneaux analysis for 3D Einstein gravity

$$\{Q[\varepsilon], Q[\eta]\} = \delta_{\varepsilon}Q[\eta]$$
$$Q[\varepsilon] \sim \oint d\varphi \mathcal{L}(\varphi)\varepsilon(\varphi)$$
$$\delta_{\varepsilon}\mathcal{L} = \mathcal{L}\varepsilon + 2\mathcal{L}\varepsilon' + \frac{\ell}{16\pi G_N}\varepsilon'''$$

Universal recipe:

- $1. \ \mbox{Identify bulk theory and variational principle}$
- 2. Fix background and impose suitable boundary conditions
- 3. Perform canonical analysis and check consistency of bc's
- 4. Derive (classical) asymptotic symmetry algebra and central charges Example: Two copies of Virasoro algebra

$$\left[\mathcal{L}_{n}, \mathcal{L}_{m}\right] = \left(n-m\right)\mathcal{L}_{n+m} + \frac{c}{12}\left(n^{3}-n\right)\delta_{n+m,0}$$

with Brown–Henneaux central charge

$$c = \frac{3\ell}{2G_N}$$

Reminder: ASA = quotient algebra of asymptotic symmetries by 'trivial' asymptotic symmetries with zero canonical charges

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- Improve to quantum ASA Example: semi-classical ASA in spin-3 gravity (Henneaux, Rey '10; Campoleoni, Pfenninger, Fredenhagen, Theisen '10)

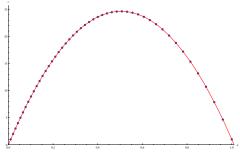
$$[W_n, W_m] = \frac{16}{5c} \sum_p L_p L_{n+m-p} + \dots$$

quantum ASA

$$[W_n, W_m] = \frac{16}{5c + 22} \sum_p : L_p L_{n+m-p} : + \dots$$

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- 5. Improve to quantum ASA
- 6. Study unitary representations of quantum ASA Example:



#### Afshar et al '12

Discrete set of Newton constant values compatible with unitarity (3D spin-N gravity in next-to-principal embedding)

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- Identify/constrain dual field theory Example: Monster CFT in (flat space) chiral gravity Witten '07
  - Li, Song & Strominger '08

Bagchi, Detournay & DG '12

$$Z(q) = J(q) = \frac{1}{q} + (1 + 196883) q + \mathcal{O}(q^2)$$

Note:  $\ln 196883 \approx 12.2 = 4\pi + \text{quantum corrections}$ 

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Goal of this talk:

Apply algorithm above to flat space holography in 3D higher spin theories

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- Example where it does not work at all: highest weight conditions!

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Many open issues in flat space holography!

(Higher spin) gravity as Chern–Simons gauge theory...

...with weird boundary conditions (Achucarro & Townsend '86; Witten '88; Bañados '96)

CS action (for AdS:  $sl(2) \oplus sl(2)$ ):

$$S_{\rm CS} = \frac{k}{4\pi} \int \mathrm{CS}(A) - \frac{k}{4\pi} \int \mathrm{CS}(\bar{A})$$

Variational principle:

$$\delta S_{\rm CS}|_{\rm EOM} = \frac{k}{4\pi} \int {\rm Tr} \left( A \wedge \delta A - \bar{A} \wedge \delta \bar{A} \right)$$

Well-defined for boundary conditions (similarly for  $\bar{A}$ )

 $A_{+} = 0$  or  $A_{-} = 0$  boundary coordinates  $x^{\pm}$ 

Example: asymptotically AdS<sub>3</sub> (Cartan-version of Brown–Henneaux)

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$$\begin{aligned} A_{\rho} &= L_{0} & \bar{A}_{\rho} &= -L_{0} \\ A_{+} &= e^{\rho} L_{1} + e^{-\rho} L(x^{+}) L_{-1} & \bar{A}_{+} &= 0 \\ A_{-} &= 0 & \bar{A}_{-} &= -e^{\rho} L_{-1} - e^{-\rho} \bar{L}(x^{-}) L_{1} \end{aligned}$$

Dreibein:  $e/\ell \sim A - \bar{A}$ , spin-connection:  $\omega \sim A + \bar{A}$ 

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Global part: contracted to isl(2) (generators:  $L_{\pm 1}, L_0, M_{\pm 1}, M_0$ )

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- ► Is precisely the (centrally extended) BMS<sub>3</sub> algebra!
- Central charges:

$$c_L = c - \bar{c}$$
  $c_M = (c + \bar{c})/\ell$ 

- ▶ Take two copies of Virasoro, generators  $\mathcal{L}_n$ ,  $\bar{\mathcal{L}}_n$ , central charges c,  $\bar{c}$
- Define superrotations  $L_n$  and supertranslations  $M_n$

$$L_n := \mathcal{L}_n - \bar{\mathcal{L}}_{-n} \qquad M_n := \frac{1}{\ell} \left( \mathcal{L}_n + \bar{\mathcal{L}}_{-n} \right)$$

 $\blacktriangleright$  Make ultrarelativistic boost,  $\ell \rightarrow \infty$ 

$$[L_n, L_m] = (n - m) L_{n+m} + c_L \frac{1}{12} \delta_{n+m,0}$$
$$[L_n, M_m] = (n - m) M_{n+m} + c_M \frac{1}{12} \delta_{n+m,0}$$
$$[M_n, M_m] = 0$$

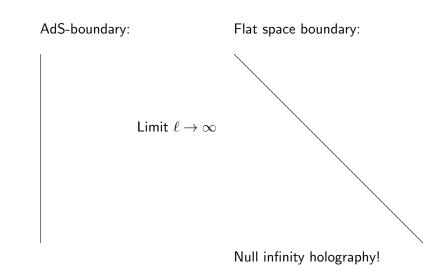
- ► Is precisely the (centrally extended) BMS<sub>3</sub> algebra!
- Central charges:

$$c_L = c - \bar{c}$$
  $c_M = (c + \bar{c})/\ell$ 

Example TMG (with gravitational CS coupling  $\mu$  and Newton constant G):

$$c_L = \frac{3}{\mu G} \qquad c_M = \frac{3}{G}$$

Consequence of ultrarelativistic boost for AdS boundary



AdS metric ( $\varphi \sim \varphi + 2\pi$ ):  $ds^2_{AdS} = d(\ell\rho)^2 - \cosh^2(\frac{\ell\rho}{\ell}) dt^2 + \ell^2 \sinh^2(\frac{\ell\rho}{\ell}) d\varphi^2$ 

AdS metric 
$$(\varphi \sim \varphi + 2\pi)$$
:  

$$ds^{2}_{AdS} = d(\ell\rho)^{2} - \cosh^{2}(\frac{\ell\rho}{\ell}) dt^{2} + \ell^{2} \sinh^{2}(\frac{\ell\rho}{\ell}) d\varphi^{2}$$
Limit  $\ell \rightarrow \infty (r = \ell\rho)$ :  

$$ds^{2}_{Flat} = dr^{2} - dt^{2} + r^{2} d\varphi^{2} = -du^{2} - 2 du dr + r^{2} d\varphi^{2}$$

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BTZ metric:

$$\mathrm{d}s_{\rm BTZ}^2 = -\frac{(\frac{r^2}{\ell^2} - \frac{r^2_+}{\ell^2})(r^2 - r^2_-)}{r^2} \, \mathrm{d}t^2 + \frac{r^2 \, \mathrm{d}r^2}{(\frac{r^2}{\ell^2} - \frac{r^2_+}{\ell^2})(r^2 - r^2_-)} + r^2 \left(\mathrm{d}\varphi - \frac{\frac{r_+}{\ell} r_-}{r^2} \, \mathrm{d}t\right)^2$$

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Limit  $\ell \to \infty$  ( $\hat{r}_+ = \frac{r_+}{\ell} = \text{finite}$ ):

$$\mathrm{d}s_{\rm FSC}^2 = \hat{r}_+^2 \left(1 - \frac{r_-^2}{r^2}\right) \,\mathrm{d}t^2 - \frac{1}{1 - \frac{r_-^2}{r^2}} \,\frac{\mathrm{d}r^2}{\hat{r}_+^2} + r^2 \left(\mathrm{d}\varphi - \frac{\hat{r}_+ \, r_-}{r^2} \,\mathrm{d}t\right)^2$$

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Shifted-boost orbifold studied by Cornalba & Costa more than decade ago Describes expanding (contracting) Universe in flat space Cosmological horizon at  $r = r_{-}$ , screening CTCs at r < 0

# Outline

Motivations

Holography basics

Flat space holography

Flat space higher spin holography

Flat space higher spin gravity

Afshar, Bagchi, Fareghbal, DG, Rosseel '13, Gonzalez, Matulich, Pino, Troncoso '13

▶ AdS gravity in CS formulation: spin 2 → spin 3  $\sim$  sl(2) → sl(3)

Flat space higher spin gravity

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AdS gravity in CS formulation: spin 2 → spin 3 ~ sl(2) → sl(3)
 Flat space: similar!

$$S_{\rm CS}^{\rm flat} = \frac{k}{4\pi} \int {\rm CS}(\mathcal{A})$$

with  $\operatorname{isl}(3)$  connection (  $e^a=\text{``zuvielbein''}$  )

$$\mathcal{A} = e^a T_a + \omega^a J_a \qquad T_a = (M_n, V_m) \quad J_a = (L_n, U_m)$$

 $\mathsf{isl}(3)$  algebra (spin 3 extension of global part of  $\mathsf{BMS}/\mathsf{GCA}$  algebra)

$$[L_n, L_m] = (n - m)L_{n+m}$$

$$[L_n, M_m] = (n - m)M_{n+m}$$

$$[L_n, U_m] = (2n - m)U_{n+m}$$

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$$[U_n, U_m] = (n - m)(2n^2 + 2m^2 - nm - 8)L_{n+m}$$

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Same type of boundary conditions as for spin 2:

$$\mathcal{A}(r, t, \varphi) = b^{-1}(r) \left( d + a(t, \varphi) + o(1) \right) b(r)$$

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Spin 3 charges:

$$Q[\varepsilon_M, \varepsilon_L, \varepsilon_V, \varepsilon_U] \sim \oint \left(\varepsilon_M(\varphi)M(\varphi) + \varepsilon_L(\varphi)L(\varphi) + \varepsilon_V(\varphi)V(\varphi) + \varepsilon_U(\varphi)U(\varphi)\right)$$

Asymptotic symmetry algebra at finite level k Afshar, Bagchi, Fareghbal, DG, Rosseel '13

▶ Do either Brown–Henneaux type of analysis or İnönü–Wigner contraction of two copies of quantum W<sub>3</sub>-algebra

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- ▶ Do either Brown–Henneaux type of analysis or İnönü–Wigner contraction of two copies of quantum W<sub>3</sub>-algebra
- ▶ Obtain new type of W-algebra as extension of BMS ("BMW")

$$\begin{split} [L_n, L_m] &= (n-m)L_{n+m} + \frac{c_L}{12} \left(n^3 - n\right) \delta_{n+m,0} \\ [L_n, M_m] &= (n-m)M_{n+m} + \frac{c_M}{12} \left(n^3 - n\right) \delta_{n+m,0} \\ [U_n, U_m] &= (n-m)(2n^2 + 2m^2 - nm - 8)L_{n+m} + \frac{192}{c_M} (n-m)\Lambda_{n+m} \\ &- \frac{96\left(c_L + \frac{44}{5}\right)}{c_M^2} (n-m)\Theta_{n+m} + \frac{c_L}{12} n(n^2 - 1)(n^2 - 4) \delta_{n+m,0} \\ [U_n, V_m] &= (n-m)(2n^2 + 2m^2 - nm - 8)M_{n+m} + \frac{96}{c_M} (n-m)\Theta_{n+m} \\ &+ \frac{c_M}{12} n(n^2 - 1)(n^2 - 4) \delta_{n+m,0} \\ \Lambda_n &= \sum_p : L_p M_{n-p} : -\frac{3}{10} (n+2)(n+3)M_n \qquad \Theta_n = \sum_p M_p M_{n-p} \end{split}$$

other commutators as in isl(3) with  $n \in \mathbb{Z}$ 

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- Note quantum shift and poles in central terms!
- $\blacktriangleright$  Analysis generalizes to flat space contractions of other W-algebras

Unitarity in flat space Unitarity leads to further contraction DG, Riegler, Rosseel '14

Facts:

• Unitarity in GCA requires  $c_M = 0$  (see paper for caveats!)

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### Higher spin states decouple and become null states!

1. NO-GO:

Generically (see paper) you can have only two out of three:

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Example:

Flat space chiral gravity Bagchi, Detournay, DG, 1208.1658

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Minimal model holography

Gaberdiel, Gopakumar, 1011.2986, 1207.6697

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Example:

Flat space higher spin gravity (Galilean  $W_3$  algebra) Afshar, Bagchi, Fareghbal, DG and Rosseel, 1307.4768 Gonzalez, Matulich, Pino and Troncoso, 1307.5651

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Compatible with "spirit" of various no-go results in higher dimensions!

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2. YES-GO:

There is (at least) one counter-example, namely a Vasiliev-type of theory, where you can have all three properties!

Unitary, non-trivial flat space higher spin algebra exists! Vasiliev-type flat space chiral higher spin gravity?

Flat space  $W_\infty$ -algebra compatible with unitarity DG, Riegler, Rosseel '14

► We do not know if flat space chiral higher spin gravity exists...

Flat space  $\mathit{W}_\infty\textsc{-algebra}$  compatible with unitarity DG, Riegler, Rosseel '14

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- ...but its existence is at least not ruled out by the no-go result!
- If it exists, this must be its asymptotic symmetry algebra:

$$\begin{bmatrix} \mathcal{V}_m^i, \mathcal{V}_n^j \end{bmatrix} = \sum_{r=0}^{\lfloor \frac{i+j}{2} \rfloor} g_{2r}^{ij}(m,n) \, \mathcal{V}_{m+n}^{i+j-2r} + c_{\mathcal{V}}^i(m) \, \delta^{ij} \, \delta_{m+n,0}$$
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where

$$c^i_{\mathcal{V}}(m) = \#(i, m) \times c$$
 and  $c = -\bar{c}$ 

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- AdS parent theory: no trace anomaly, but gravitational anomaly (Like in conformal Chern–Simons gravity → Vasiliev type analogue?)

Long story short:

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 $A_u \to A_u + \mu$ 

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 $A_u \to A_u + \mu$ 

Works nicely in Chern–Simons formulation! Line-element with spin-2 and spin-3 chemical potentials:

$$g_{\mu\nu} dx^{\mu} dx^{\nu} = \left( r^{2} \left( \mu_{\rm L}^{2} - 4\mu_{\rm U}^{\prime\prime} \mu_{\rm U} + 3\mu_{\rm U}^{\prime 2} + 4\mathcal{M}\mu_{\rm U}^{2} \right) + r g_{uu}^{(r)} + g_{uu}^{(0)} + g_{uu}^{(0')} \right) du^{2} + \left( r^{2} \mu_{\rm L} - r\mu_{\rm M}^{\prime} + \mathcal{N}(1 + \mu_{\rm M}) + 8\mathcal{Z}\mu_{\rm V} \right) 2 du d\varphi - (1 + \mu_{\rm M}) 2 dr du + r^{2} d\varphi^{2} g_{uu}^{(0)} = \mathcal{M}(1 + \mu_{\rm M})^{2} + 2(1 + \mu_{\rm M})(\mathcal{N}\mu_{\rm L} + 12\mathcal{V}\mu_{\rm V} + 16\mathcal{Z}\mu_{\rm U}) + 16\mathcal{Z}\mu_{\rm L}\mu_{\rm V} + \frac{4}{3}(\mathcal{M}^{2}\mu_{\rm V}^{2} + 4\mathcal{M}\mathcal{N}\mu_{\rm U}\mu_{\rm V} + \mathcal{N}^{2}\mu_{\rm U}^{2})$$

Spin-3 field with same chemical potentials:

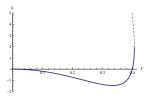
$$\begin{split} \Phi_{\mu\nu\lambda} \, \mathrm{d}x^{\mu} \, \mathrm{d}x^{\nu} \, \mathrm{d}x^{\lambda} &= \Phi_{uuu} \, \mathrm{d}u^{3} + \Phi_{ruu} \, \mathrm{d}r \, \mathrm{d}u^{2} + \Phi_{uu\varphi} \, \mathrm{d}u^{2} \, \mathrm{d}\varphi - \left(2\mu_{\mathrm{U}}r^{2} - r\mu_{\mathrm{V}}' + 2\mathcal{N}\mu_{\mathrm{V}}\right) \mathrm{d}r \, \mathrm{d}u \, \mathrm{d}\varphi \\ &+ \mu_{\mathrm{V}} \, \mathrm{d}r^{2} \, \mathrm{d}u - \left(\mu_{\mathrm{U}}'r^{3} - \frac{1}{3}r^{2}(\mu_{\mathrm{V}}'' - \mathcal{M}\mu_{\mathrm{V}} + 4\mathcal{N}\mu_{\mathrm{U}}) + r\mathcal{N}\mu_{\mathrm{V}}' - \mathcal{N}^{2}\mu_{\mathrm{V}}\right) \mathrm{d}u \, \mathrm{d}\varphi^{2} \end{split}$$

$$\begin{split} \Phi_{uuu} &= r^2 \left[ 2(1+\mu_{\rm M}) \mu_{\rm U} (\mathcal{M}\mu_{\rm L} - 4\mathcal{V}\mu_{\rm U}) - \frac{1}{3} \mu_{\rm L}^2 (\mathcal{M}\mu_{\rm V} - 4\mathcal{N}\mu_{\rm U}) + 16\mu_{\rm L}\mu_{\rm U} (\mathcal{V}\mu_{\rm V} + \mathcal{Z}\mu_{\rm U}) - \frac{4}{3} \mathcal{M}\mu_{\rm U}^2 (\mathcal{M}\mu_{\rm V} + 2\mathcal{M}\mu_{\rm U}) \right] \\ &+ 2\mathcal{N}\mu_{\rm U}) \right] + 2\mathcal{V}(1+\mu_{\rm M})^3 + \frac{2}{3} (1+\mu_{\rm M})^2 (6\mathcal{Z}\mu_{\rm L} + \mathcal{M}^2\mu_{\rm V} + 2\mathcal{M}\mathcal{N}\mu_{\rm U}) + 16\mu_{\rm L}\mu_{\rm V}^2 (\mathcal{N}\mathcal{V} - \frac{1}{3}\mathcal{M}\mathcal{Z}) \\ &+ \frac{2}{3} (1+\mu_{\rm M}) ((\mathcal{N}\mu_{\rm L} + 16\mathcal{Z}\mu_{\rm U}) (2\mathcal{M}\mu_{\rm V} + \mathcal{N}\mu_{\rm U}) + 12\mathcal{M}\mathcal{V}\mu_{\rm V}^2) + \frac{64}{3} \mathcal{Z}\mu_{\rm U}\mu_{\rm V} (\mathcal{N}\mu_{\rm L} + 12\mathcal{V}\mu_{\rm V} + 12\mathcal{Z}\mu_{\rm U}) \\ &+ \mathcal{N}^2 \mu_{\rm L}^2 \mu_{\rm V} + 64\mathcal{V}^2 \mu_{\rm V}^3 - \frac{8}{27} (\mathcal{M}^3 \mu_{\rm V}^3 - \mathcal{N}^3 \mu_{\rm U}^3) - \frac{4}{9} \mathcal{M}\mathcal{N}\mu_{\rm U}\mu_{\rm V} (4\mathcal{M}\mu_{\rm V} + 5\mathcal{N}\mu_{\rm U}) + \sum_{n=0}^3 r^n \Phi_{uuu}^{(r^n)} \end{split}$$

Long story short:

 $A_u \to A_u + \mu$ 

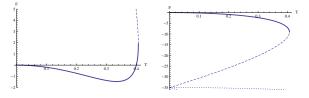
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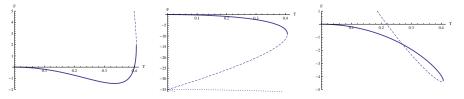
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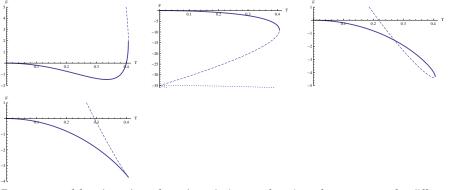
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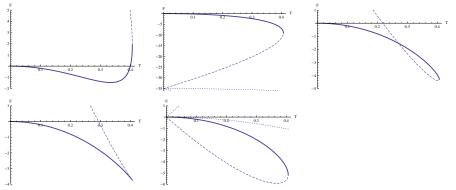
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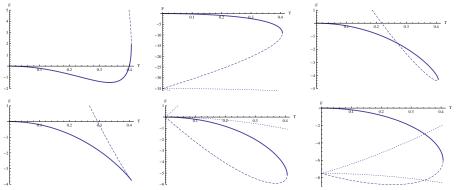
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Flat space higher spin holography provides a new playground Contributes to long-term goal: find how general is holography

# Thanks for your attention!



Daniel Grumiller — Flat space higher spin holography