## Three-dimensional gravity and logarithmic CFT Nordic Network Meeting, Göteborg



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## Outline

## Logarithmic CFT

Lightning review
LCFTs as limits
Gravity duals
Early hints
Candidate theories
Tests of the conjectures
TMG
NMG
GMG
Conclusion

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- Reviews: [Flohr] hep-th/0111228, [Gaberdiel hep-th/0111260


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with

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D^{L / R}=\not \partial \pm \frac{1}{\ell} \quad D^{m}=\not \partial+\mu
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$D^{m} \psi^{m}=0$ is a massive graviton. $\psi^{L / R}$ are "pure gauge" $\sim T_{z z} / T_{\bar{z} \bar{z}}$.

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- Conjecture: $\mu \ell=1$ is dual to an LCFT!


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- Add $\frac{1}{\mu} S_{C S}$ : Generalised Massive Gravity. Around $\mathrm{AdS}_{3}$ :

$$
\left(D^{L} D^{R} D^{m_{1}} D^{m_{2}} \psi\right)_{\mu \nu}=0 \quad m_{1,2} \ell=\frac{m^{2} \ell^{2}}{2 \mu \ell} \pm \sqrt{\frac{1}{2}-\sigma m^{2} \ell^{2}+\frac{m^{4} \ell^{4}}{4 \mu^{2} \ell^{2}}} .
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## GMG parameter space

- $D^{m_{1}}=D^{L}$ :
$T_{z z}$ has log-partner!
- $D^{m_{1}}=D^{m_{2}}$ :
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- $D^{m_{1}}=D^{m_{2}}=D^{L}$ :

Rank 3 Jordan cell!

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- 1-loop partition function consistent with LCFT. [Gaberdiel, Grumiller, Sachs '10]


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